

GCE Examinations

Further Pure Mathematics Module FP1

Advanced Subsidiary / Advanced Level

Paper C

Time: 1 hour 30 minutes

Instructions and Information

Candidates may use any calculator except those with a facility for symbolic algebra and/or calculus.

Full marks may be obtained for answers to ALL questions.

Mathematical and statistical formulae and tables are available.

This paper has 7 questions.

Advice to Candidates

You must show sufficient working to make your methods clear to an examiner.
Answers without working will gain no credit.



Written by Shaun Armstrong & Chris Huffer

© Solomon Press

These sheets may be copied for use solely by the purchaser's institute.

1. Find the set of values of x for which

$$|x - 2| > 2|x + 1|. \quad (6 \text{ marks})$$

2. (a) By using the substitution $y = vx$, or otherwise, find the general solution of the differential equation

$$xy \frac{dy}{dx} = x^2 + y^2. \quad (7 \text{ marks})$$

- (b) Given also that $y = 2$ when $x = 1$, show that for $x > 0$

$$y^2 = 2x^2(\ln x + 2). \quad (2 \text{ marks})$$

3. (a) Find the sum of the series

$$2^3 + 4^3 + 6^3 + \dots + (2n)^3,$$

giving your answer in a simplified form. (3 marks)

- (b) Hence, or otherwise, show that the sum of the series

$$1^3 - 2^3 + 3^3 - 4^3 + \dots + (2n - 1)^3 - (2n)^3$$

is $-n^2(4n + 3)$. (6 marks)

4. Find the general solution of the differential equation

$$\frac{d^2y}{dx^2} - 6\frac{dy}{dx} + 9y = 2e^{3x}. \quad (10 \text{ marks})$$

5.

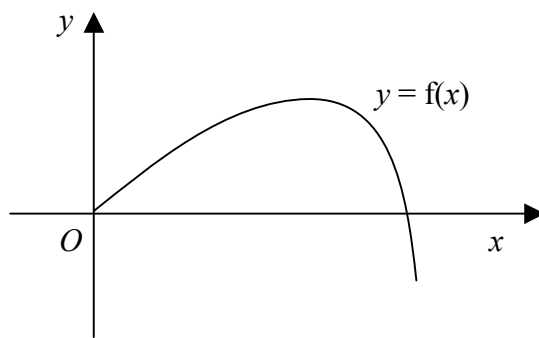


Fig. 1

Figure 1 shows part of the curve $y = f(x)$ where

$$f(x) \equiv 2x - \tan x, \quad x \in \mathbb{R}, \quad 0 \leq x < \frac{\pi}{2}.$$

- (a) Show that there is a root, α , of the equation $f(x) = 0$ in the interval $(1, 1.5)$. **(2 marks)**
- (b) Use the Newton-Raphson method with an initial value of $x = 1.25$ to find α correct to 2 decimal places and justify the accuracy of your answer. **(7 marks)**
- (c) Explain with the aid of a diagram why the Newton-Raphson method fails if an initial value of $x = 0.75$ is used when trying to find α . **(3 marks)**

6. The complex numbers z and w are defined such that

$$\begin{aligned} 3z + w &= 14, \text{ and} \\ z - iw &= 15 - 9i. \end{aligned}$$

- (a) Show that $z = 3 - 4i$ and find w in the form $a + ib$, where a and b are real numbers. **(6 marks)**
- (b) Find the square roots of z in the form $c + id$, where c and d are real numbers. **(7 marks)**

Turn over

7.

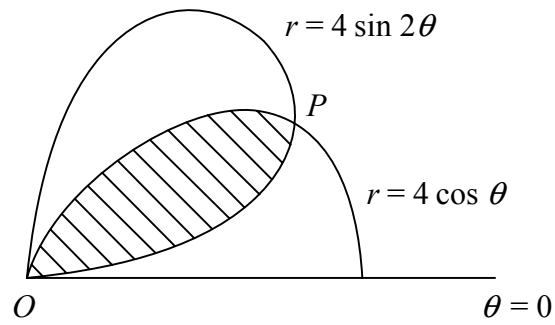


Fig. 2

Figure 2 shows the curves with polar equations

$$r = 4 \sin 2\theta \quad 0 \leq \theta \leq \frac{\pi}{2},$$

$$r = 4 \cos \theta \quad 0 \leq \theta \leq \frac{\pi}{2}.$$

- (a) Find the polar coordinates of the point P where the two curves intersect. **(5 marks)**
- (b) Find the exact area of the shaded region bounded by the two curves. **(11 marks)**

END